

# Interpreting, Training, and Distilling Seq2Seq Models

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(with Yoon Kim, Sam Wiseman, Hendrik Strobelt, Yuntian Deng, Allen Schmalz)

<http://www.github.com/harvardnlp/seq2seq-talk/>



at



**Carnegie Mellon University**  
Language Technologies Institute

## Sequence-to-Sequence

- Machine Translation (Kalchbrenner and Blunsom, 2013; Sutskever et al., 2014b; Cho et al., 2014; Bahdanau et al., 2014; Luong et al., 2015)
- Question Answering (Hermann et al., 2015)
- Conversation (Vinyals and Le, 2015) (Serban et al., 2016)
- Parsing (Vinyals et al., 2014)
- Speech (Chorowski et al., 2015; Chan et al., 2015)
- Caption Generation (Karpathy and Li, 2015; Xu et al., 2015; Vinyals et al., 2015)
- Video-Generation (Srivastava et al., 2015)
- NER/POS-Tagging (Gillick et al., 2016)
- Summarization (Rush et al., 2015)

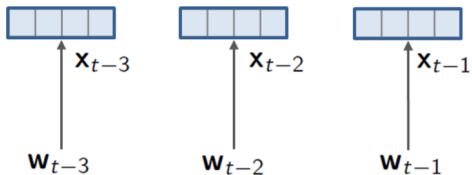
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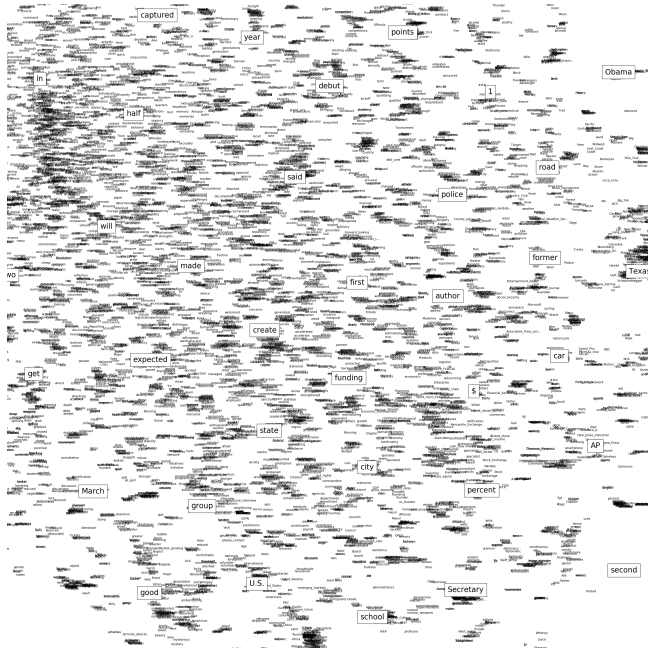
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## Seq2Seq Neural Network Toolbox

Embeddings	sparse features	$\Rightarrow$	dense features
RNNs	feature sequences	$\Rightarrow$	dense features
Softmax	dense features	$\Rightarrow$	discrete predictions

Embeddings      sparse features     $\Rightarrow$     dense features

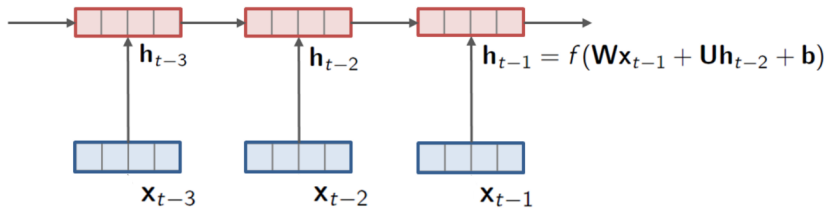




[Words Vectors]

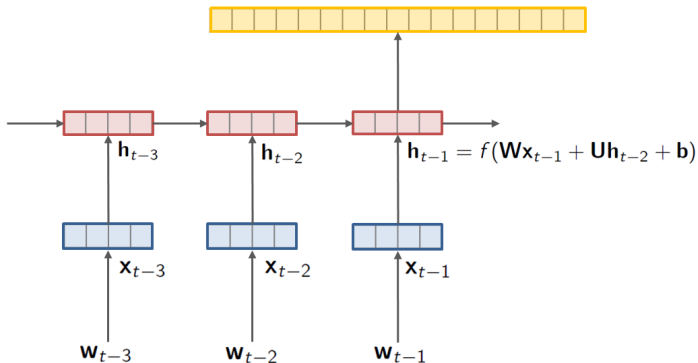
RNNs/LSTMs

feature sequences  $\Rightarrow$  dense features



LM/Softmax

dense features  $\Rightarrow$  discrete predictions

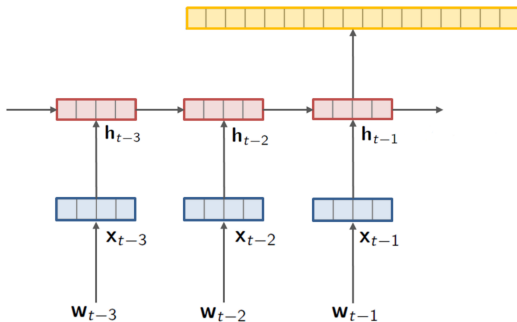


$$p(w_t | w_1, \dots, w_{t-1}; \theta) = \text{softmax}(\mathbf{W}_{out} \mathbf{h}_{t-1} + \mathbf{b}_{out})$$

$$p(w_{1:T}) = \prod_t p(w_t | w_1, \dots, w_{t-1})$$



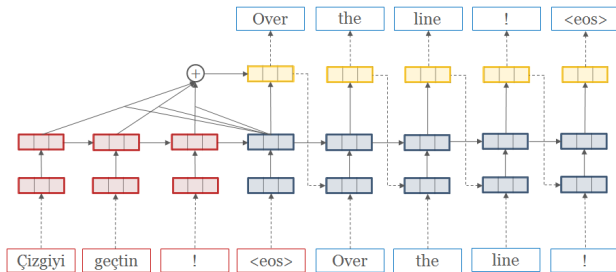
## Contextual Language Model / “seq2seq”



- Key idea, contextual language model based on encoder  $x$ :

$$p(w_{1:T}|x) = \prod_t p(w_t|w_1, \dots, w_{t-1}, x)$$

## Actual Seq2Seq / Encoder-Decoder / Attention-Based Models



- Different encoders, attention mechanisms, input feeding, ...
- Almost all models use LSTMs or other gated RNNs
- Large multi-layer networks necessary for good performance.
  - 4 layer, 1000 hidden dims is common for MT

# Seq2Seq-Attn

- HarvardNLP's open-source system (Yoon Kim)  
<http://github.com/harvardnlp/seq2seq-attn>
- Used by SYSTRAN for 32 language pairs (Crego et al., 2016)

## Text Translation

*This demo platform allows you to experience Pure Neural™ machine translation based on the last Research community's findings and SYSTRAN's R&D. You can translate up to 2000 characters of text in the languages proposed below. Check out the [information page](#) to learn more.*

The screenshot displays the SYSTRAN Text Translation demo interface. At the top, there is a header bar with a language selection dropdown set to 'English', a 'Filter' button, and a 'Select a profile' button. Below this, the main area is divided into three sections: a large text input area on the left labeled 'Translation on the internet', a central translation area labeled 'Übersetzung im Internet', and a sidebar on the right. The sidebar contains a list of translation services with checkboxes and progress bars, including 'translation', 'Übersetzung', 'english translation', 'certified translation', 'French translation', 'machine translation', 'on', 'darüber', 'spät', 'danach', and 'danach'. The interface is designed to allow users to input text and see the translation results in real-time.

## Seq2Seq Applications: Neural Summarization (Rush et al., 2015)

### Source (First Sentence)

*Russian Defense Minister Ivanov called Sunday for the creation of a joint front for combating global terrorism.*

### Target (Title)

*Russia calls for joint front against terrorism.*

- (Mou et al., 2015) (Cheng and Lapata, 2016) (Toutanova et al., 2016) (Wang et al., 2016b) (Takase et al., 2016), among others
- Used by Washington Post to suggest headlines (Wang et al., 2016a)

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## Seq2Seq Applications: Grammar Correction (Schmaltz et al., 2016)

### Source (Original Sentence)

*There is no a doubt, tracking systems has brought many benefits in this information age .*

### Target (Corrected Sentence)

*There is no doubt, tracking systems have brought many benefits in this information age .*

- 1st on BEA'11 grammar correction task (Daudaravicius et al., 2016)

## Seq2Seq Applications: Im2Markup (Deng and Rush, 2016)

$$r = \frac{\sqrt{Q_3}}{l} \sin \left( \frac{l}{\sqrt{Q_3}} u \right),$$

[Latex Example]

[Project]

## This Talk

- How can we **interpret** these learned hidden representations?
- How should we **train** these style of models?
- How can we **shrink** these models for practical applications?

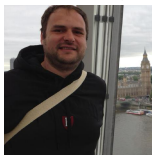


## This Talk

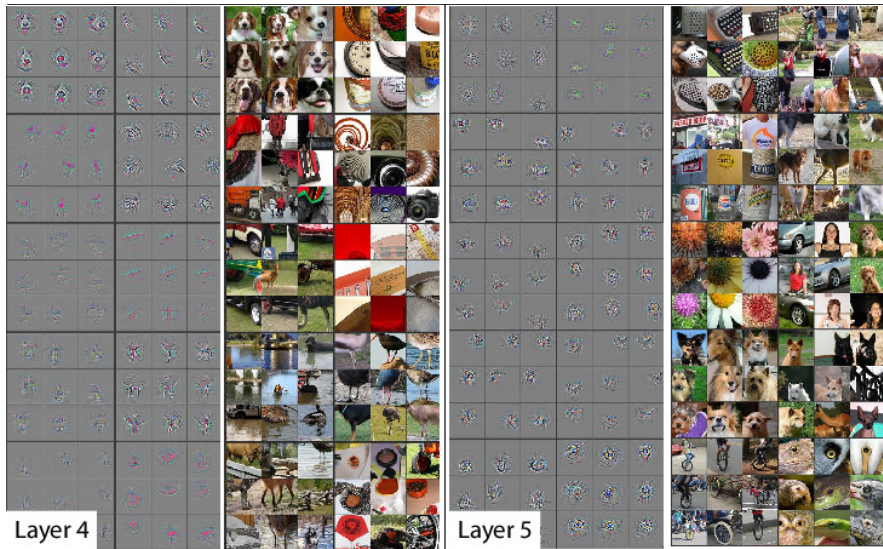
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LSTMVis [lstm.seas.harvard.edu](http://lstm.seas.harvard.edu)

(Strobelt et al., 2016)

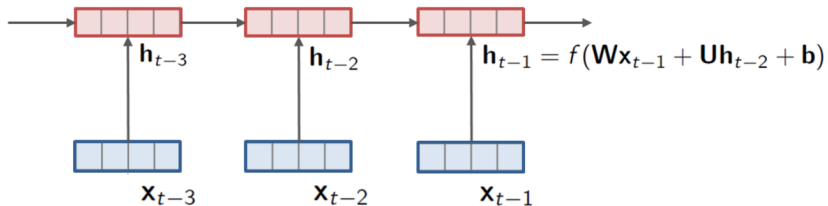
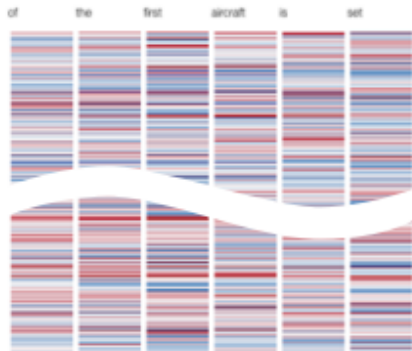


- How should we **train** these style of models? (Wiseman and Rush, 2016)
- How can we **shrink** these models for practical applications? (Kim and Rush, 2016)



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# Vector-Space RNN Representation



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(Karpathy et al., 2015)

### Example 1: Synthetic (Finite-State) Language

alphabet: ( ) 0 1 2 3 4

corpus: ( 1 ( 2 ) ( ) ) 0 ( ( ( 3 ) ) 1 )

- Numbers are randomly generated, must match nesting level.
- Train a predict-next-word language model (decoder-only).

$$p(w_t | w_1, \dots, w_{t-1})$$

[Parens Example]

## Example 2: Real Language

alphabet: all english words

corpus: Project Gutenberg Children's books

- Train a predict-next-word language model (decoder-only).

$$p(w_t | w_1, \dots, w_{t-1})$$

[LM Example]

### Example 3: Seq2Seq Encoder

alphabet: all english words

corpus: Summarization

- Train a full seq2seq model, examine *encoder* LSTM.

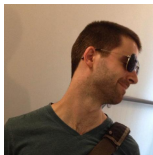
[Summarization Example]

## This Talk

- How can we **interpret** these learned hidden representations?  
(Strobelt et al., 2016)
- How should we **train** these style of models?

### Sequence-to-Sequence Learning as Beam-Search Optimization

(Wiseman and Rush, 2016)



- How can we **shrink** these models for practical applications (Kim and Rush, 2016)?



## Seq2Seq Notation

- $x$ ; source input
- $\mathcal{V}$ ; vocabulary
- $w_t$ ; random variable for the  $t$ -th target token with support  $\mathcal{V}$
- $y_{1:T}$ ; ground-truth output
- $\hat{y}_{1:T}$ ; predicted output
- $p(w_{1:T} \mid x; \theta) = \prod_t p(w_t \mid w_{1:t-1}, x; \theta)$ ; model distribution

## Seq2Seq Details

**Train Objective:** Given source-target pairs  $(x, y_{1:T})$ , minimize NLL of each word independently, conditioned on *gold* history  $y_{1:t-1}$

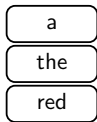
$$\mathcal{L}_{\text{NLL}}(\theta) = - \sum_t \log p(w_t = y_t | y_{1:t-1}, x; \theta)$$

**Test Objective:** Structured prediction

$$\hat{y}_{1:T} = \arg \max_{w_{1:T}} \sum_t \log p(w_t | w_{1:t-1}, x; \theta)$$

- Typical to approximate the  $\arg \max$  with beam-search

## Beam Search ( $K = 3$ )



For  $t = 1 \dots T$ :

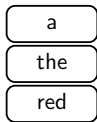
- For all  $k$  and for all possible output words  $w$ :

$$s(w, \hat{y}_{1:t-1}^{(k)}) \leftarrow \log p(\hat{y}_{1:t-1}^{(k)} | x) + \log p(w | \hat{y}_{1:t-1}^{(k)}, x)$$

- Update beam:

$$\hat{y}_{1:t}^{(1:K)} \leftarrow \text{K-arg max } s(w, \hat{y}_{1:t-1}^{(k)})$$

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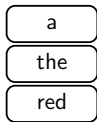
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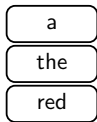
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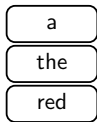
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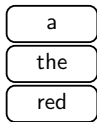
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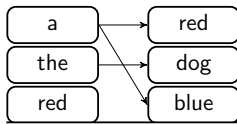
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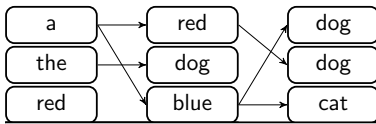
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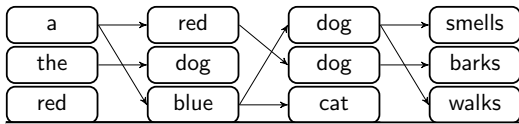
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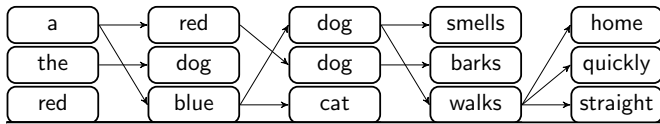
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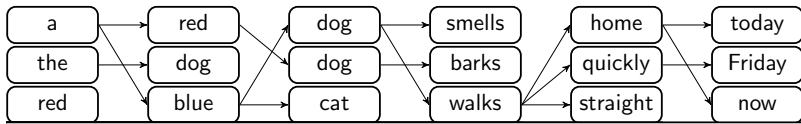
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## Problem

How should we train sequence models?

## Related Work

- Approaches to Exposure Bias, Label Bias:
  - Data as Demonstrator, Scheduled Sampling (Venkatraman et al., 2015; Bengio et al., 2015)
  - Globally Normalized Transition-Based Networks (Andor et al., 2016)
- RL-based approaches
  - MIXER (Ranzato et al., 2016)
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**Issue #1: Train/Test Mismatch** (cf., (Ranzato et al., 2016))

$$\text{NLL}(\theta) = - \sum_t \log p(w_t = y_t | y_{1:t-1}, x; \theta)$$

- (a) Training conditions on *true* history (“Exposure Bias”)
- (b) Train with word-level NLL, but evaluate with BLEU-like metrics

**Idea #1:** Train with beam-search

- Use a loss that incorporates sequence-level costs



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**BSO Idea #1:** Use a loss that incorporates sequence-level costs

$$\mathcal{L}(\theta) = \sum_t \Delta(\hat{y}_{1:t}^{(K)}) \left[ 1 - s(y_t, y_{1:t-1}) + s(\hat{y}_t^{(K)}, \hat{y}_{1:t-1}^{(K)}) \right]$$

- $y_{1:t}$  is the gold prefix;  $\hat{y}_{1:t}^{(K)}$  is the  $K$ 'th prefix on the beam
- $\Delta(\hat{y}_{1:t}^{(K)})$  allows us to scale loss by badness of predicting  $\hat{y}_{1:t}^{(K)}$

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**Issue #2: Seq2Seq models next-word probabilities:**

$$s(w, \hat{y}_{1:t-1}^{(k)}) \leftarrow \log p(\hat{y}_{1:t-1}^{(k)} | x) + \log p(w | \hat{y}_{1:t-1}^{(k)}, x)$$

- (a) Sequence score is sum of locally normalized word-scores; gives rise to “Label Bias” (Lafferty et al., 2001)
- (b) What if we want to train with sequence-level constraints?

**Idea #2:** Don't locally normalize

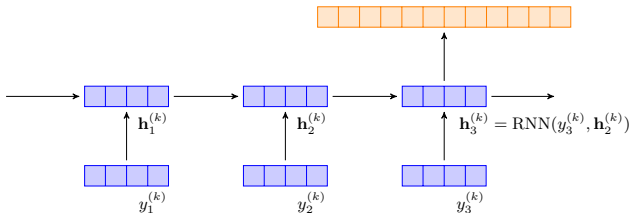
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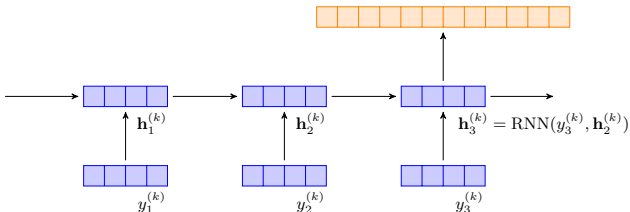
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$$s(w, \hat{y}_{1:t-1}^{(k)}) = \log p(\hat{y}_{1:t-1}^{(k)} | x) + \log \text{softmax}(\mathbf{W}_{out} \mathbf{h}_{t-1}^{(k)} + \mathbf{b}_{out})$$

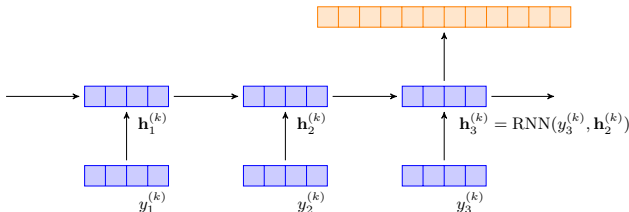


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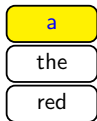
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- Can set  $s(w, \hat{y}_{1:t-1}^{(k)}) = -\infty$  if  $(w, \hat{y}_{1:t-1}^{(k)})$  violates a hard constraint

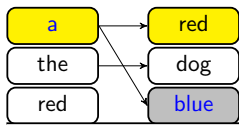
## Beam Search Optimization



$$\mathcal{L}(\theta) = \sum_t \Delta(\hat{y}_{1:t}^{(K)}) \left[ 1 - s(y_t, y_{1:t-1}) + s(\hat{y}_t^{(K)}, \hat{y}_{1:t-1}^{(K)}) \right]$$

- Color Gold: target sequence  $y$
- Color Gray: violating sequence  $\hat{y}^{(K)}$

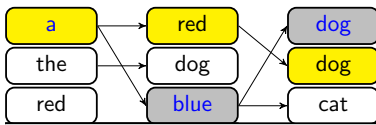
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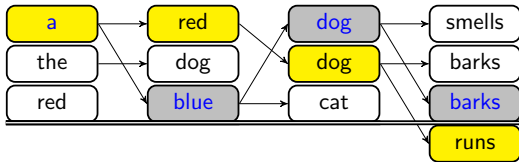
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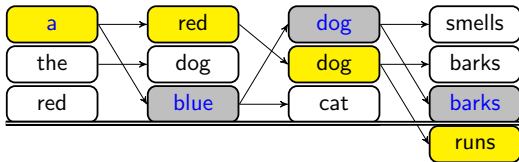
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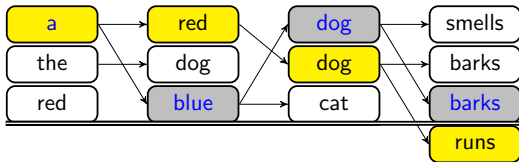


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- If no margin violation at  $t - 1$ , update beam as usual
- Otherwise, update beam with sequences prefixed by  $y_{1:t-1}$

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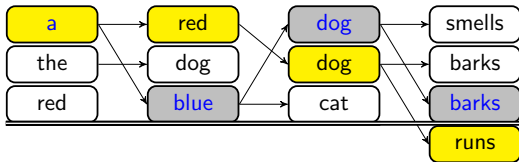
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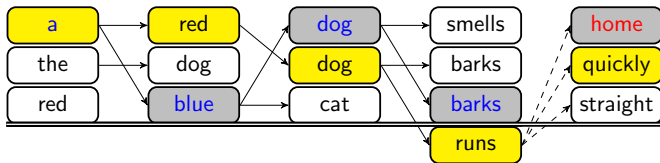


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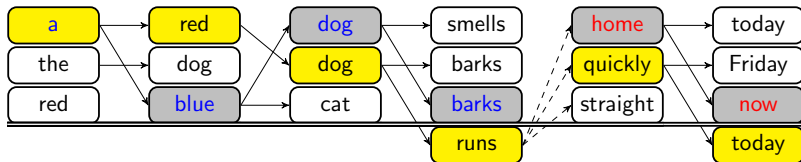


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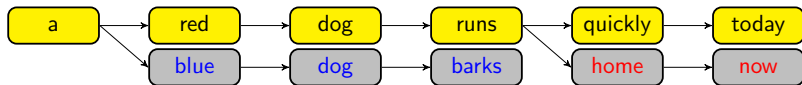
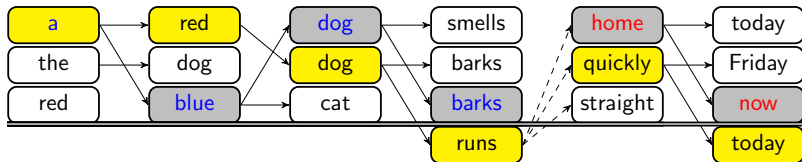


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- Otherwise, update beam with sequences prefixed by  $y_{1:t-1}$

## Backpropagation over Structure



## Experiments

- Word Ordering, Dependency Parsing, Machine Translation
- Uses LSTM encoders and decoders, attention, input feeding
- All models trained with Adagrad (Duchi et al., 2011)
- Pre-trained with NLL;  $K$  increased gradually
- “BSO” uses unconstrained search; “ConBSO” uses constraints

	$K_e = 1$	$K_e = 5$	$K_e = 10$
Word Ordering (BLEU)			
seq2seq	25.2	29.8	31.0
BSO	28.0	33.2	34.3
ConBSO	<b>28.6</b>	<b>34.3</b>	<b>34.5</b>
Dependency Parsing (UAS/LAS) <sup>1</sup>			
seq2seq	<b>87.33/82.26</b>	88.53/84.16	88.66/84.33
BSO	86.91/82.11	91.00/ <b>87.18</b>	91.17/ <b>87.41</b>
ConBSO	85.11/79.32	<b>91.25</b> /86.92	<b>91.57</b> /87.26
Machine Translation (BLEU)			
seq2seq	22.53	24.03	23.87
BSO, SB- $\Delta$ , $K_t=6$	<b>23.83</b>	<b>26.36</b>	<b>25.48</b>
XENT	17.74	20.10	20.28
DAD	20.12	22.25	22.40
MIXER	20.73	21.81	21.83

<sup>1</sup>Note Andor et al. (2016) have SOA, with 94.41/92.55.

## This Talk

- How can we **interpret** these learned hidden representations?  
(Strobelt et al., 2016)
- How should we **train** these style of models? (Wiseman and Rush, 2016)
- How can we **shrink** these models for practical applications?

## Sequence-Level Knowledge Distillation

(Kim and Rush, 2016)





Google unleashes deep learning tech on language with **Neural** ...

[TechCrunch](#) - Sep 27, 2016

Google has been working on a **machine learning translation** technique for years, and today is its official debut. The Google **Neural Machine** ...

Google **Translate** now converts Chinese into English with **neural** ...

[VentureBeat](#) - Sep 27, 2016

Google announces **Neural Machine Translation**

[The Stack](#) - Sep 28, 2016

Google announces **Neural Machine Translation** to improve Google ...

Highly Cited - [ZDNet](#) - Sep 27, 2016

Google is using **Neural Networks** for Chinese to English **machine** ...

Opinion - [Firstpost](#) - Sep 28, 2016

Google announces **neural** network to improve **machine translation**

In-Depth - [Seeking Alpha](#) - Sep 27, 2016



ZDNet



VentureBeat



The Stack



Geektime



Ubergizmo



Science Mag...

[View all](#)

SYSTRAN: 1st software provider to launch a **Neural Machine** ...

[GlobeNewswire](#) (press release) - Oct 17, 2016

In December, SYSTRAN will communicate the feedback received on Pure **Neural**™ **Machine Translation**, its roadmap and time to market plan ...

Iconic Integrates Custom **Neural Machine Translation** Into ...

[Slator](#) (press release) (subscription) - Oct 6, 2016

Dublin – October 6, 2016 – Iconic **Translation Machines** (Iconic), a leading Irish **machine translation** (MT) software and solutions provider, today ...





## Neural Machine Translation

Excellent results on many language pairs, but need large models

- Original seq2seq paper (Sutskever et al., 2014a): 4-layers/1000 units
- Deep Residual RNNs (Zhou et al., 2016) : 16-layers/512 units
- Google's NMT system (Wu et al., 2016): 8-layers/1024 units

Beam search + ensemble on top

⇒ Deployment is challenging!

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## Related Work: Compressing Deep Models

- **Pruning:** Prune weights based on importance criterion (LeCun et al., 1990; Han et al., 2016; See et al., 2016)
- **Knowledge Distillation:** Train a *student* model to learn from a *teacher* model (Bucila et al., 2006; Ba and Caruana, 2014; Hinton et al., 2015; Kuncoro et al., 2016). (Sometimes called “dark knowledge”)

## Knowledge Distillation (Bucila et al., 2006; Hinton et al., 2015)

- Train a *larger teacher* model first to obtain teacher distribution  $q(\cdot)$
- Train a *smaller student* model  $p(\cdot)$  to mimic the teacher

### Word-Level Knowledge Distillation

Teacher distribution:  $q(w_t | y_{1:t-1})$

$$\mathcal{L}_{\text{NLL}} = - \sum_t \sum_{k \in \mathcal{V}} \mathbb{1}\{y_t = k\} \log p(w_t = k | y_{1:t-1}; \theta)$$

$$\mathcal{L}_{\text{WORD-KD}} = - \sum_t \sum_{k \in \mathcal{V}} q(w_t = k | y_{1:t-1}) \log p(w_t = k | y_{1:t-1}; \theta)$$

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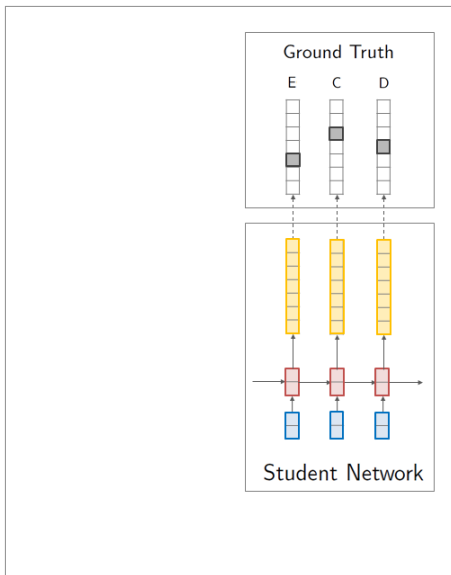
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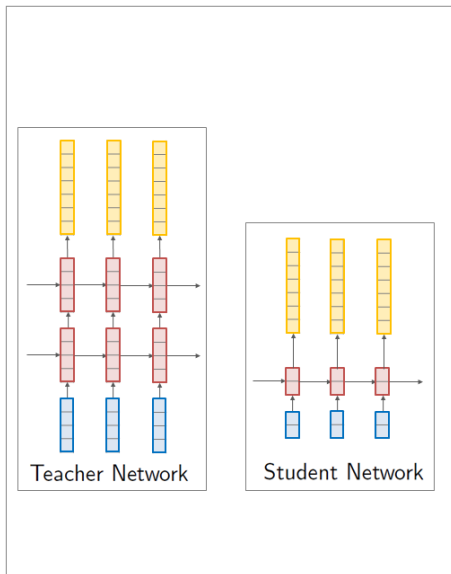
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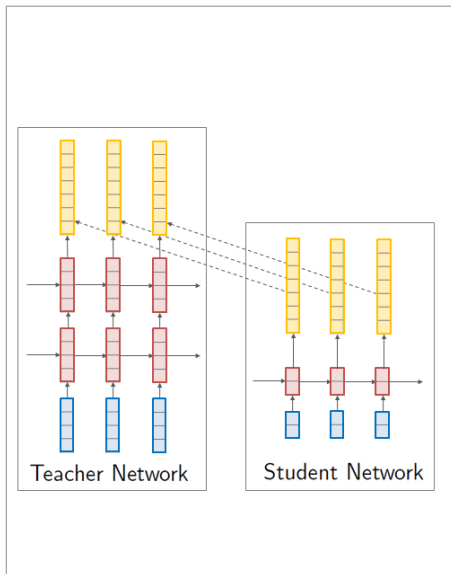
## No Knowledge Distillation



## Word-Level Knowledge Distillation



## Word-Level Knowledge Distillation





## Word-Level Knowledge Distillation Results

English  $\rightarrow$  German (WMT 2014)

Model	BLEU
$4 \times 1000$ Teacher	19.5
$2 \times 500$ Baseline (No-KD)	17.6
$2 \times 500$ Student (Word-KD)	17.7
$2 \times 300$ Baseline (No-KD)	16.9
$2 \times 300$ Student (Word-KD)	17.6

## This Work: Sequence-Level Knowledge Distillation

$$\mathcal{L}_{\text{NLL}} = - \sum_t \sum_{k \in \mathcal{V}} \mathbb{1}\{y_t = k\} \log p(w_t = k \mid y_{1:t-1})$$

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Instead minimize cross-entropy, between  $q$  and  $p$  implied *sequence*-distributions

$$\mathcal{L}_{\text{SEQ-KD}} = - \sum_{w_{1:T} \in \mathcal{V}^T} q(w_{1:T} \mid x) \log p(w_{1:T} \mid x)$$

Sum over an exponentially-sized set  $\mathcal{V}^T$ .

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## Sequence-Level Knowledge Distillation

Approximate  $q(w \mid x)$  with mode

$$q(w_{1:T} \mid x) \approx \mathbb{1}\{\arg \max_{w_{1:T}} q(w_{1:T} \mid x)\}$$

Approximate mode with beam search

$$\hat{y} \approx \arg \max_{w_{1:T}} q(w_{1:T} \mid x)$$

Simple model: train the student model on  $\hat{y}$  with NLL

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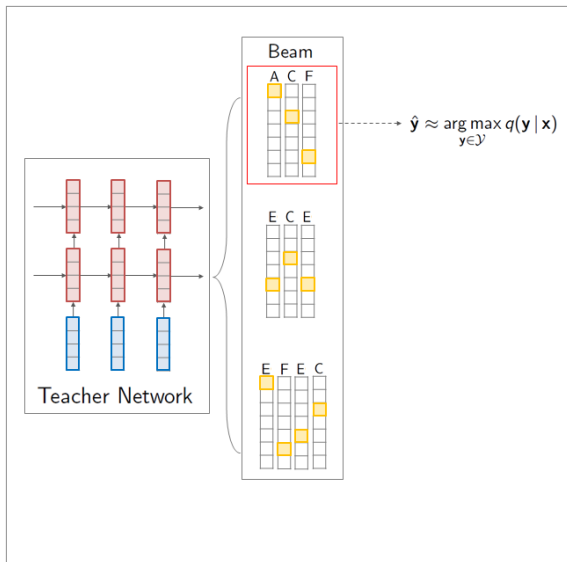
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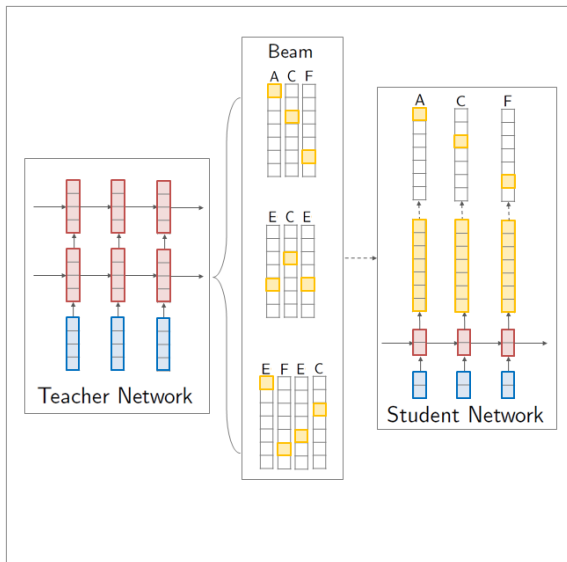
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# Sequence-Level Knowledge Distillation



## Sequence-Level Knowledge Distillation





## Sequence-Level Interpolation

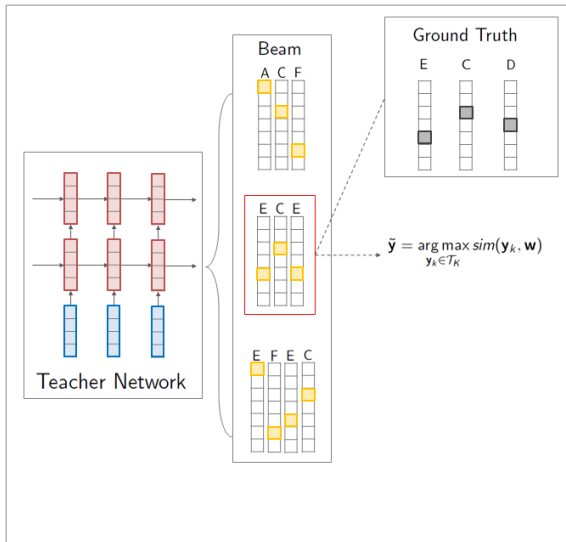
Word-level knowledge distillation

$$\mathcal{L} = \alpha \mathcal{L}_{\text{WORD-KD}} + (1 - \alpha) \mathcal{L}_{\text{NLL}}$$

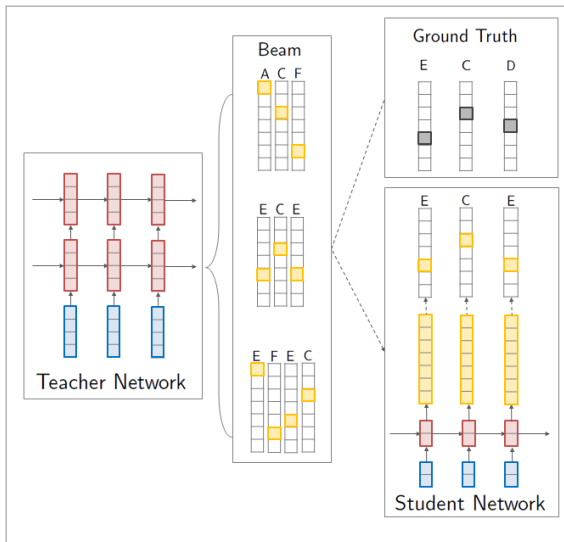
Training the student towards the mixture of teacher/data distributions.

How can we incorporate ground truth data at the sequence-level?

## Sequence-Level Interpolation



## Sequence-Level Interpolation



## Experiments on English $\rightarrow$ German (WMT 2014)

- Word-KD: Word-level Knowledge Distillation
- Seq-KD: Sequence-level Knowledge Distillation with beam size  $K = 5$
- Seq-Inter: Sequence-level Interpolation with beam size  $K = 35$ .  
Fine-tune from pretrained Seq-KD (or baseline) model with smaller learning rate.





Results: English  $\rightarrow$  German (WMT 2014)

Model	BLEU <sub>K=1</sub>	$\Delta_{K=1}$	BLEU <sub>K=5</sub>	$\Delta_{K=5}$	PPL	$p(\hat{\mathbf{y}})$
$4 \times 1000$						
Teacher	17.7	—	19.5	—	6.7	1.3%
$2 \times 500$						
Student	14.7	—	17.6	—	8.2	0.9%
Word-KD	15.4	+0.7	17.7	+0.1	8.0	1.0%
Seq-KD	18.9	+4.2	19.0	+1.4	22.7	16.9%





# Results: English $\rightarrow$ German (WMT 2014)

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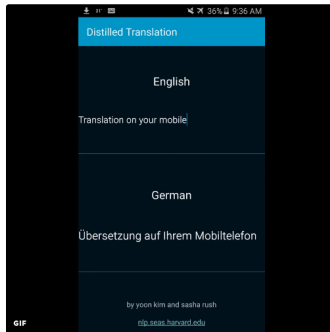
Many more experiments (different language pairs, combining configurations, different sizes etc.) in paper

# An Application



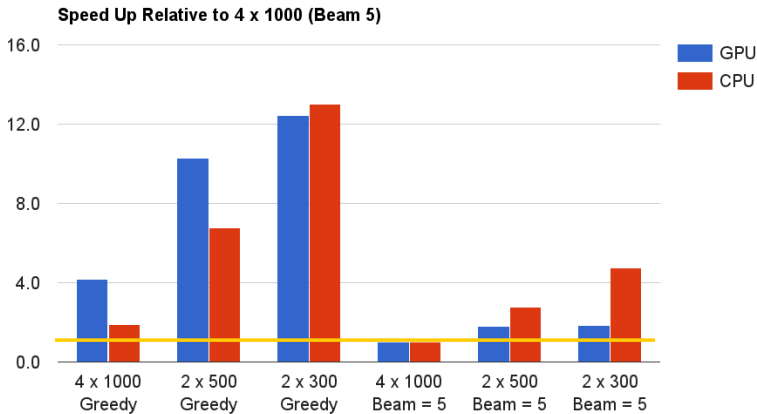
harvardnlp  
@harvardnlp

Seq KD ([arxiv.org/abs/1606.07947](https://arxiv.org/abs/1606.07947)): learn small LSTMs for fast translation. Runs on a phone ([nlp.seas.harvard.edu/translation.apk](http://nlp.seas.harvard.edu/translation.apk))



[App]

# Decoding Speed



## Combining Knowledge Distillation and Pruning

Number of parameters still large for student models (mostly due to word embedding tables)

- $4 \times 1000$ : 221 million
- $2 \times 500$ : 84 million
- $2 \times 300$ : 49 million

Prune student model: Same methodology as See et al. (2016)

- Prune  $x\%$  of weights based on absolute value
- Fine-tune pruned model (crucial!)

## Combining Knowledge Distillation and Pruning

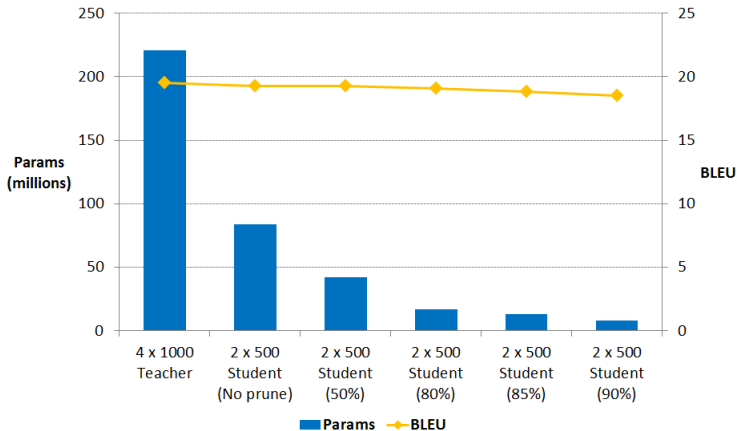
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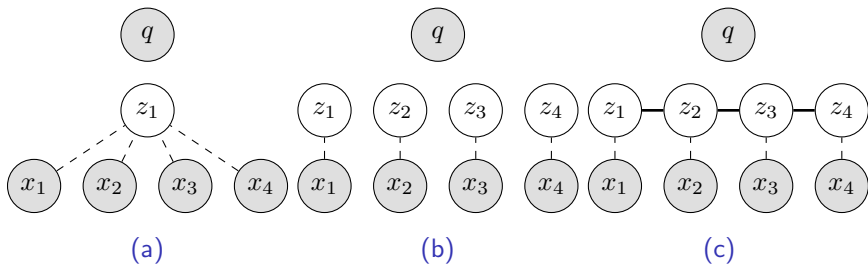
## Conclusion: Other work

- How can we **interpret** these learned hidden representations?
  - Lei et al. (2016) other methods for interpreting decisions (as opposed to states).
- How should we **train** these style of models?
  - Lee et al. (2016) CCG parsing (backprop through search is a thing now/again)
- How can we **shrink** these models for practical applications?
  - Live deployment: (greedy) student outperforms (beam search) teacher. (Crego et al., 2016)
  - Can compress an ensemble into a single model (Kuncoro et al., 2016)



## Coming Work

- Structured Attention Networks (Kim et al 2016)



Thanks!

# References I

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